

# Optimizing Nonlinear Optical Visibility of Two-Dimensional Materials

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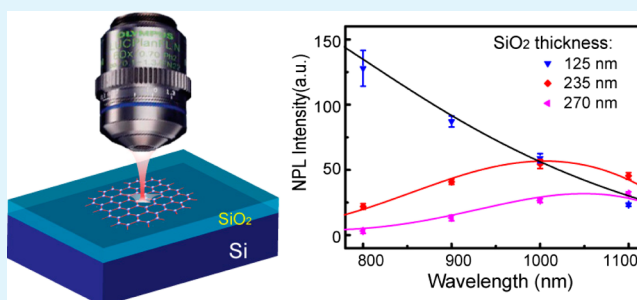
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## Supporting Information

**ABSTRACT:** Two-dimensional (2D) materials have attracted broad research interests across various nonlinear optical (NLO) studies, including nonlinear photoluminescence (NPL), second harmonic generation (SHG), transient absorption (TA), and so forth. These studies have unveiled important features and information of 2D materials, such as in grain boundaries, defects, and crystal orientations. However, as most research studies focused on the intrinsic NLO processes, little attention has been paid to the substrates underneath. Here, we discovered that the NLO signal depends significantly on the thickness of SiO<sub>2</sub> in SiO<sub>2</sub>/Si substrates. A 40-fold enhancement of the NPL signal of graphene was observed when the SiO<sub>2</sub> thickness was varied from 270 to 125 nm under 800 nm excitation. We systematically studied the NPL intensity of graphene on three different SiO<sub>2</sub> thicknesses within a pump wavelength range of 800–1100 nm. The results agreed with a numerical model based on back reflection and interference. Furthermore, we have extended our measurements to include TA and SHG of graphene and MoS<sub>2</sub>, confirming that SiO<sub>2</sub> thickness has similar effects on all of the three major types of NLO signals. Our results will serve as an important guidance for choosing the optimum substrates to conduct NLO research studies on 2D materials.

**KEYWORDS:** nonlinear optics, two-dimensional materials, nonlinear optical microscopy, transient absorption, nonlinear photoluminescence, SiO<sub>2</sub> thickness



## 1. INTRODUCTION

Two-dimensional (2D) materials have drawn enormous research attentions owing to their unique electrical, optical, and chemical properties. For instance, the “Dirac cone” band structure of graphene results in its high mobility, quantum Hall effect, and Klein tunneling effect;<sup>1</sup> the valley structure of transition metal dichalcogenide (TMDC) has boosted the research studies of “valleytronics”;<sup>2</sup> and the more recent black phosphorus (BP) has unique electronic property and strong anisotropy.<sup>3,4</sup> As a result, these 2D materials have shown excellent device performances such as in field-effect transistors, integrated circuits, solar cells, and light-emitting diodes.<sup>5–8</sup> Furthermore, various van der Waals heterostructures can be constructed with these 2D materials, where the interactions between them could influence their electronic and optoelectronic properties,<sup>9</sup> leading to a rapidly growing research area.<sup>10–12</sup>

Although atomically thin, many 2D materials have demonstrated exotic optical responses. In linear optics, the universal absorbance ( $e^2/4h$ ) of single-layer graphene is well-known;<sup>13</sup> TMDCs such as single-layered MoS<sub>2</sub> have shown strong and valley-selective photoluminescence (PL);<sup>14,15</sup> and BP has demonstrated layer-dependent exciton emissions.<sup>16–18</sup>

In nonlinear optics, a rapidly growing interest has been focused on various nonlinear optical (NLO) properties of 2D materials, which are usually orders of magnitude stronger than conventional bulk materials.<sup>19–21</sup> These NLO processes could be divided into three major categories. First, coherent optical parametric processes, such as second harmonic generation (SHG),<sup>22</sup> third harmonic generation (THG), and four-wave mixing (FWM).<sup>23,24</sup> For instance, graphene generates strong THG and FWM signals, whereas MoS<sub>2</sub> has unique SHG property that reflects its crystal symmetry in mono- and few-layered samples. Second, nonlinear dissipative processes, including transient absorption (TA), two-photon absorption (TPA), and saturable absorption, that pump electrons into an excited state.<sup>25–29</sup> In particular, TA could be used to learn the transient dynamics of excited photocarriers through a pump-probe-based method and reveal ultrafast electron–electron or electron–phonon interactions. Third, incoherent photon up-conversion processes, such as two-photon fluorescence of MoS<sub>2</sub> and nonlinear PL (NPL) of graphene.<sup>30–32</sup> All of these NLO

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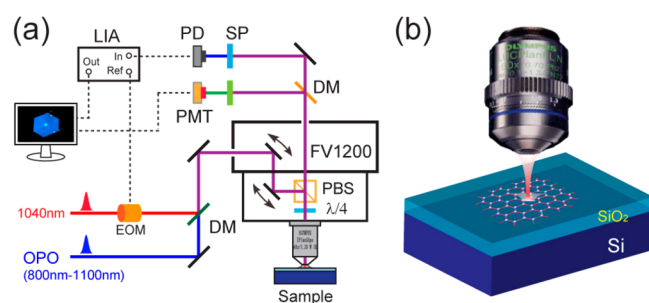
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properties of 2D materials have been explored and utilized in optical microscopy, both for material and biological sciences.<sup>33–36</sup>

Despite extensive studies, the relationship between the NLO intensity of 2D materials and the thickness of their substrates has never been seriously investigated, whereas the thickness-dependent linear optical contrast of graphene has been well-studied and applied to optimize its visibility.<sup>37,38</sup> In fact, the choice of SiO<sub>2</sub>/Si substrates used for the NLO measurements appears quite random throughout the literature studies. Three major commercially available thicknesses of SiO<sub>2</sub> have been used: 90, 200, and 285 nm, even for measuring the same 2D material.<sup>3,39–42</sup> Besides, large discrepancies exist among experiments measuring the same NLO susceptibility of graphene with the same SiO<sub>2</sub> thickness but different excitation wavelengths.<sup>23,43,44</sup> Therefore, it is worth quantifying the relationship between the NLO intensities of 2D materials and the underneath SiO<sub>2</sub> thickness. Here, we carefully measured the NPL intensities of graphene as functions of the SiO<sub>2</sub> thickness and excitation wavelength, the results of which were explained by our numerical model based on the interference of the excitation laser. The interference between the forward and back-reflected beams creates partial standing waves that have varying intensity profiles in the sample planes, depending on the SiO<sub>2</sub> thickness. We chose NPL because it is dominated by the incoherent process that requires only one excitation beam and thus simplifies the modeling. More than 1 order of magnitude difference could be seen between different SiO<sub>2</sub> thicknesses, proving the crucial role of such an effect in NLO signal generation, which was underestimated previously. Furthermore, we have extended our measurements to include the other two major types of NLO processes—TA of graphene and SHG of MoS<sub>2</sub>. Compared with linear optics and NPL, additional factors need to be taken into account, such as the coherence of SHG emission and the interaction between pump and probe beams in TA measurements. Our simplified model could qualitatively agree with all of the above experimental results and may aid future NLO research studies of 2D materials.

## 2. EXPERIMENTAL SECTION

**2.1. Optical Apparatus.** We constructed a multimodality NLO microscopy system to measure the three types of NLO signals on synthesized graphene and MoS<sub>2</sub>. The optical setup of the microscope system is shown in Figure 1, similar to the ones reported



**Figure 1.** Schematics of the experimental design. (a) Optical setup of the NLO microscope. (b) Cartoon illustration of the focused laser beam onto the 2D materials on the Si/SiO<sub>2</sub> substrate. EOM: electro-optical modulator; LIA: lock-in amplifier; DM: dichroic mirror; PD: photodiode; PMT: photomultiplier tube; SP: short-pass optical filter; and PBS: polarizing beam splitter.

previously.<sup>34,36,45</sup> Two laser beams from a femtosecond optical parametric oscillator (OPO, InSight DS+, Newport, CA) were used as the light source for our NLO microscope. For NPL or SHG measurements, the tunable OPO output (800–1100 nm) was used to excite the samples, and the emission photons were collected through the same microscope objective, filtered by proper optical filters and detected with a photomultiplier tube (PMT). We used a short-pass filter (FF01-750SP, Semrock) for NPL measures and a narrow band-pass filter (FF01-405/10, Semrock) for SHG detection with 810 nm excitation. For TA measurements, a pump-probe-based optical setup was built, in which the fundamental 1040 nm beam was used as the pump, and the OPO output as the probe. Both beams were overlapped spatially and temporally, sent into the laser-scanning microscope (FV1200, Olympus), and focused onto the samples. To efficiently collect the back-reflected probe beam, a polarizing beam splitter (PBS) and a quarter wave plate were inserted before the objective lens. The intensity of the pump beam was modulated at 20 MHz by an electro-optical modulator (EOM). The probe beam was optically filtered, collected by a photodiode (PD), and demodulated with a commercial lock-in amplifier (HF2LI, Zurich Instruments) to extract the TA signals. All of the NLO signals were connected to the microscope inputs to form images. The 2D materials on different substrates were imaged with an air objective [UPLSAPO 20X, numerical aperture (NA) = 0.75, Olympus]. A cartoon illustration of light focusing onto 2D materials on top of the SiO<sub>2</sub>/Si substrate is shown in Figure 1b. Laser powers at the samples were kept around 2 mW. Each 512 × 512 image was taken in ~1 s, with 2 μs pixel dwell time. No detectable change of the NLO signal strength was observed during the measurements, indicating little sample degradation.

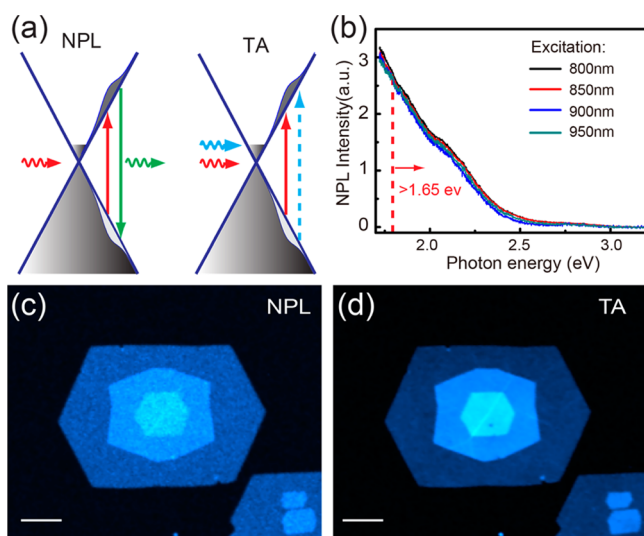
The three commercial SiO<sub>2</sub>/Si substrates mentioned above were used to conduct the thickness-dependent NLO measurements, with the measured thicknesses of 125, 235, and 270 nm using an ellipsometer (UVISEL-2, Horiba). To clarify, we only analyzed the signal intensities of monolayer materials throughout the work, unless specifically stated.

**2.2. Synthesis of Graphene.** Single-crystal graphene synthesis and transfer processes are described as follows. A standard 1 in. quartz tube in a chemical vapor deposition (CVD) furnace was used as the reaction chamber. An electropolished 25 μm thick Cu foil (99.8%, Alfa Aesar) was used for growth. The cleaned Cu foil was annealed at 1050 °C for 1 h. Then, CH<sub>4</sub> (50 sccm of 1:99 CH<sub>4</sub>/Ar mix) was added for a desired period of growth time. After the reaction, the samples were rapidly cooled to room temperature. Poly(methyl methacrylate) (43982PMMA, Alfa Aesar)-assisted method was used to transfer single-crystal graphene onto different substrates.

**2.3. Synthesis of MoS<sub>2</sub>.** MoS<sub>2</sub> was synthesized in a standard 1 in. quartz tube and a two-zone CVD equipment to control the temperature of MoO<sub>3</sub> (99.9%, Aladdin) and S (99.5%, Sinopharm Chemical Reagent Co., Ltd.), respectively. MoO<sub>3</sub> (10 mg) and Te (30 mg, 99.999%, Sinopharm Chemical Reagent Co., Ltd.) powders were physically mixed and then placed in a ceramic boat at the center of the furnace. The Te powder was used to accelerate the volatilization of MoO<sub>3</sub> during growth.<sup>46</sup> The cleaned substrate with a different thickness of SiO<sub>2</sub> was placed facing down on the ceramic boat. Sulfur powder (>500 mg) was put at the center of another heating zone, which was about 20 cm upstream from the MoO<sub>3</sub> and Te mixture. Before heating, the whole CVD equipment was vacuumed and purged with 200 sccm N<sub>2</sub> for 30 min. The reaction occurred at 1 atm pressure, with 30 sccm N<sub>2</sub> as the carrying gas. The furnace was heated to 600 °C at a rate of 20 °C/min and then increased to 800 °C at a rate of 5 °C/min. When the temperature of the furnace reached 800 °C, sulfur powder was heated to 120 °C and held for 10 min and then increased to 150 °C and held for 30 min. The sulfur source was further heated to 170 °C and held for 10 min before cooling down to 120 °C. The furnace was cooled down from 800 °C to room temperature rapidly by opening the furnace. The whole CVD system was home built in a fume hood to prevent possible leakage of sulfur and related volatile gases.

### 3. RESULTS AND DISCUSSION

We first investigated NPL and TA processes of monolayer graphene, the energy diagrams and optical transitions of which are illustrated in Figure 2a. In our measurements, the



**Figure 2.** Characterization of NPL and TA in graphene. (a) Energy diagrams and optical transitions of NPL and TA processes, the red arrows represent photoexcitation, the green arrow represents luminescence, and the blue-dashed arrow represents TA. (b) Measured NPL spectra excited at various wavelengths. Red arrow indicates our detection band (<750 nm). A typical (c) NPL and (d) TA image of a graphene crystal. Scale bar: 10 μm.

normalized NPL spectra under different excitation wavelengths are shown in Figure 2b. As can be seen, almost identical spectral shapes were generated within our detection window (1.65–3.26 eV), which would simplify our data analysis and modeling. Representative images of NPL and TA generated from the same graphene crystal are shown in Figure 2c,d, respectively. Layer number dependences of these two types of NLO signals and TA dynamics are shown in Figure S1.

We systematically studied NPL intensities of CVD-grown monolayer graphene transferred onto different SiO<sub>2</sub>/Si substrates. Although the gapless graphene does not luminesce under the excitation of continuous wave laser, it could easily emit broadband NPL far exceeding the photon energy of the femtosecond-excitation laser pulses. The NPL process was considered to be dominated by incoherent radiation from the hot carriers that are generated within tens of femtoseconds upon photoexcitation (Figure 2a).<sup>30,47</sup> The strong electron–electron and electron–phonon scatterings result in broad distribution of the hot thermalized carriers, with the emission spectra similar to that of thermal radiation.<sup>30</sup> The power dependence of the NPL signal showed a nonlinear relationship of  $\sim P^{2.1}$  (Figure 3a), which agrees with previous studies.<sup>47</sup> For each sample, we applied four excitation wavelengths: 800, 900, 1000, and 1100 nm, under fixed excitation power (2 mW on sample) and detection conditions. Significant variations of NPL intensities at different SiO<sub>2</sub> thicknesses and excitation wavelengths were observed, and the full data set is plotted in Figure 3b; each data point represents measurements from 10 samples. Under 800 nm excitation, the mean intensity ratio of monolayer graphene on the above three substrates was about 39.5:6.8:1.0. By contrast, the ratio changed to around

1.0:2.1:1.5 under 1100 nm excitation, with representative images shown in Figure 3c. The large variation of the NPL signal indicates the importance of choosing proper substrates to achieve best sensitivity and data quality.

Because the interface between graphene and SiO<sub>2</sub> remained the same, we suspect that the main contribution to the signal variation was from the interference between the forward and reflected light beams from the SiO<sub>2</sub>/Si interface, which form partial standing waves in the focal region. The constructive or destructive interference at the graphene plane results in a drastic enhancement or decrease of excitation strength, leading to the large differences observed in luminescence intensities. A similar effect was applied to realize super-resolution fluorescence microscopy using mirror substrates with various SiO<sub>2</sub> thicknesses on top.<sup>48</sup> We, thus, constructed a theoretical model based on the above considerations. First, the focusing of light field through an objective lens could be expressed as<sup>49</sup>

$$E_0(v, u) = A_0 \exp(ikz) \int_0^1 \exp\left\{-\frac{i u \rho^2}{2}\right\} J_0(\rho v) \rho \, d\rho \quad (1)$$

where  $v = kr \sin \alpha$  and  $u = 4kz \sin^2(\alpha/2)$ ;  $k = 2\pi/\lambda$  is the wave vector;  $J_0$  is the zeroth-order Bessel functions;  $\alpha$  is the aperture angle of the objective;  $r$  and  $z$  are the radial and axial coordinates at the image plane, respectively, and  $\rho$  represents the reduced coordinate at the pupil plane.<sup>49</sup> Then, the reflected field from the SiO<sub>2</sub>/Si interface was included to interfere with the incoming beam and resulted in the intensity profile of the excitation beam.<sup>48</sup>

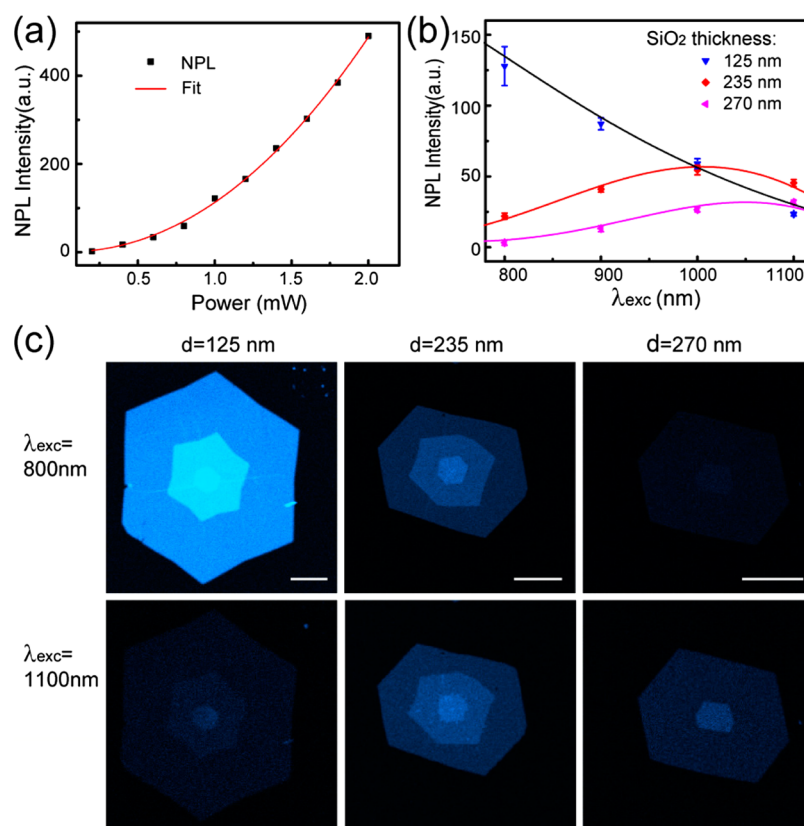
$$E(v, u)_{\text{exc}} = E_0(v, u) + \gamma \exp(i2knd)E_0(v, -u) \quad (2)$$

where  $d$  and  $n$  are the thickness and index of refraction of SiO<sub>2</sub>, respectively.  $\gamma$  is the reflection coefficient of the electric field at the SiO<sub>2</sub>/Si interface, determined by Fresnel equations under the approximation of normal incidence, because the wave fronts become plane waves at the waist of the Gaussian beams. The dispersion of both SiO<sub>2</sub> and Si was considered to calculate the wavelength-dependent  $\gamma$ ,<sup>37</sup> as shown in Figure S2. In addition, the calculated electric field in eq 2 could be readily converted to excitation intensity,  $I_{\text{exc}}$ . Because of their nonlinearity, emission intensities of NLO processes obey nonlinear power laws, which could be determined experimentally.

$$I_{\text{emi}} \propto \eta(\lambda) I_{\text{exc}}^\beta \quad (3)$$

where  $\eta$  represents the detection efficiency which depends on the excitation wavelength and  $\beta$  is the index number. In our NPL experiment,  $\eta$  originates from the wavelength-dependent emission efficiency within our fixed detection window (Figure 2b). We simulated the intensity profiles of 800 and 1100 nm excitation in the  $x$ – $z$  plane, as shown in Figure 4a. For 800 nm excitation, our results indicate a constructive interference at the sample plane with 125 nm SiO<sub>2</sub>, whereas 235 and 270 nm SiO<sub>2</sub> introduce destructive interferences and result in a much weaker NPL. However, when we changed the excitation wavelength to 1100 nm, the 235 nm substrate provides a more constructive interference, thus generating a higher NPL signal, which agrees well with our experimental results (Figure 3c). The detected signal could be calculated by integrating the emission intensity over the sample plane ( $z = 0$ ). The above model could simulate NPL intensities as functions of excitation wavelength and SiO<sub>2</sub> thickness (Figure 4b), with a constant  $\eta = 1$ . This could only predict the intensity ratios between different SiO<sub>2</sub> thicknesses under fixed excitation wavelengths but does not provide precise





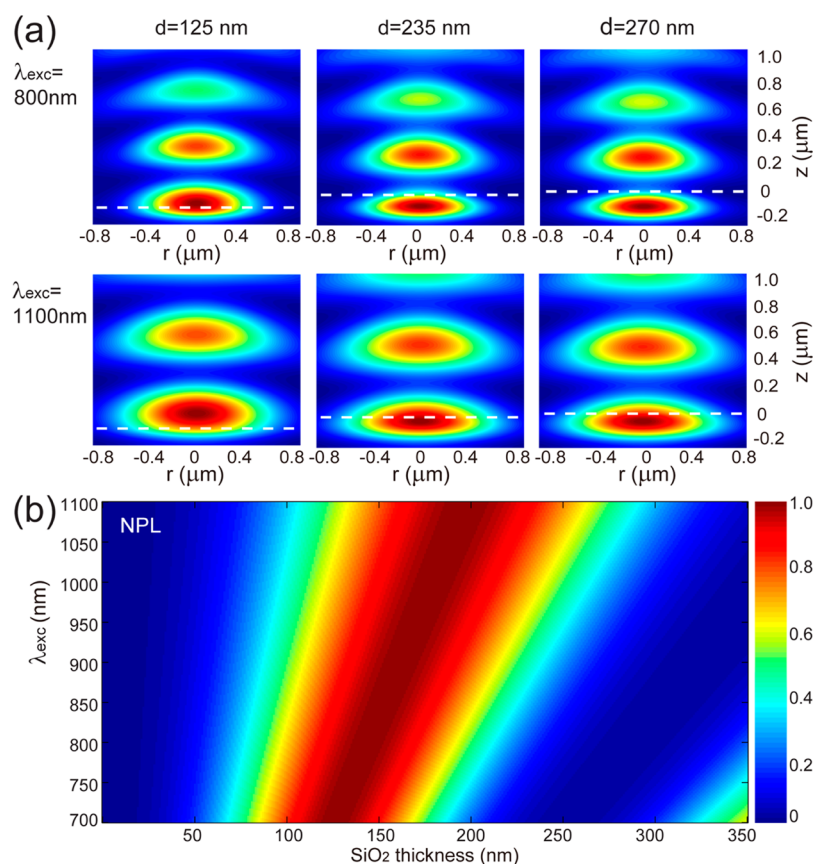
**Figure 3.** NPL properties in graphene with different substrates. (a) Laser power dependence of the NPL signal. (b) Measured NPL intensity at various excitation wavelengths and SiO<sub>2</sub> thicknesses, with simulation results plotted as solid curves. (c) Selected raw NPL images of graphene under 800 and 1100 nm excitations. Scale bar: 20  $\mu$ m.

wavelength-dependent values. Accurate formulation of  $\eta(\lambda)$  would require more profound physical models to simulate the NPL emission spectra and intensities under different excitation wavelengths and is beyond the scope of this study. By observing the close-to-linear behavior of the wavelength-dependent NPL signal at  $d = 125$  nm, we applied a phenomenological linear function of  $\eta(\lambda)$  as the global fitting parameter with the fitted result:  $\eta(\lambda) = -0.002\lambda + 2.6$  (Figure S3). This indicates that lower excitation energies result in weaker emission intensity within our fixed detection window, which also implies lower effective emission temperature.<sup>30</sup> The final simulated results agree well with the whole experimental data set, as illustrated in Figure 3b.

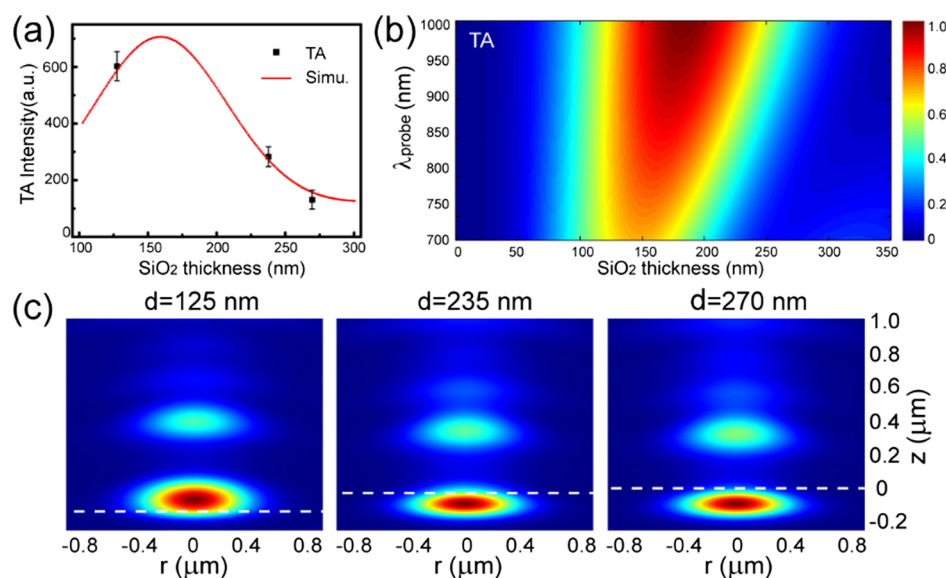
Next, we investigated the effect of SiO<sub>2</sub> thickness on the TA signal. TA is a specific type of pump-probe spectroscopy that detects the differential absorbance of the probe beam induced by pump excitation. In graphene, the photoexcited hot carriers reduce the absorption of the probe beam, resulting in the increase of its intensity, and the difference signal is used to measure the strength of TA (Figure 2a). In our study, all TA data were taken under 1040 nm pump and 800 nm probe. The quadratic power dependence of TA intensity (Figure S4) reveals its third-order nonlinearity and could be described as:  $S \propto [c] \cdot \sigma \cdot I_{pump} \cdot I_{probe}$ .<sup>50</sup> The phonon-assisted relaxation of hot carriers causes a rapid decay of the TA signal within around 2 ps, as indicated in our time-resolved TA decay curves (Figure S1), which agrees with previous results.<sup>35</sup> Peak intensities of the TA curves were used to represent their signal strengths in this study. We measured the TA strengths of graphene on the three types of substrates, resulting in a mean intensity ratio around

2.9:2.0:1 (Figure 5a). To simulate the TA signal, our model needs to include both the pump and probe intensity profiles as results of interferences and take their product to represent the TA intensity. The simulated results are included in Figure 5a, and the calculated wavelength and SiO<sub>2</sub> thickness-dependent TA signal is shown in Figure 5b. Although the overall thickness dependence of TA signals appears in a similar trend as NPL, the magnitude of change is much smoother because the different pump and probe wavelengths partially smear out the variation. The intensity profiles of the product of pump and probe focal areas are calculated with different substrate thicknesses and are shown in Figure 5c.

We also briefly studied SHG intensities of monolayer MoS<sub>2</sub> on different thicknesses of SiO<sub>2</sub>. Because SHG requires inversion symmetry breaking, we can no longer use graphene to study SHG. To minimize the polarization dependence of SHG strength of the anisotropic MoS<sub>2</sub>,<sup>33</sup> we used circular polarized light to excite the samples and detected the SHG signal without any analyzer. A typical SHG image of monolayer MoS<sub>2</sub> is shown in Figure 6a. The measured mean intensity ratio between different SiO<sub>2</sub> thicknesses is around 7.5:3.5:1, as indicated in Figure 6b. In our experiments, the excitation wavelength was fixed at 810 nm, and the SHG wavelength was 405 nm. Because SHG is a coherent process, the thin MoS<sub>2</sub> sheet (much thinner than the coherence length) generates similar amounts of SHG photons in both forward and backward directions with well-defined phase relations. Thus, the interference between the backward- and forward-reflected SHG photons has also been considered. The calculation of such interference is the same as in eq 2, with the electric field



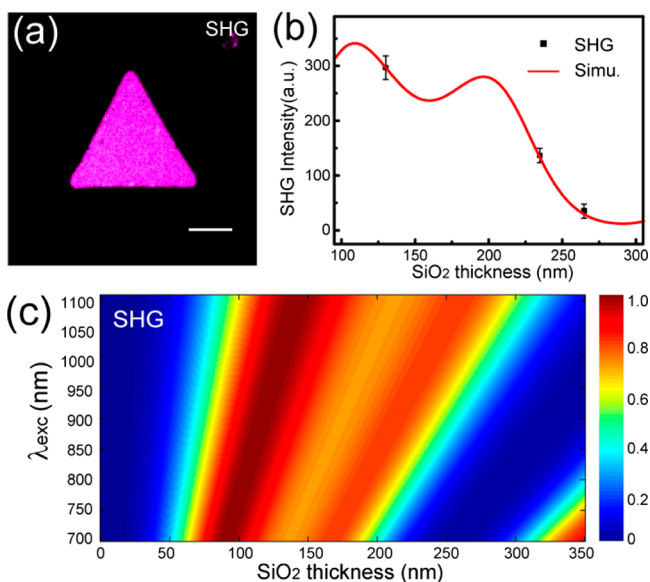
**Figure 4.** Simulation results for NPL. (a) Laser intensity profiles in the  $r$ - $z$  plane near laser focus for different SiO<sub>2</sub> thicknesses, where the sample planes are marked by the dashed lines. (b) Calculated NPL signal strength as functions of the excitation wavelength and SiO<sub>2</sub> thickness, assuming constant emission efficiency.



**Figure 5.** SiO<sub>2</sub> thickness-dependent TA signals. (a) Measured and simulated TA signals. (b) Calculated TA intensities as functions of probe wavelength and SiO<sub>2</sub> thickness. (c) Simulated intensity profiles of  $I_{pump} \cdot I_{probe}$  for different SiO<sub>2</sub> thicknesses near laser focus. The dashed lines represent sample planes.

replaced by the SHG field and the phase and reflection coefficient adjusted according to the SHG wavelength. Taking account of the interferences of both excitation and emission beams, we could calculate the angular distribution of SHG intensities integrated over a solid angle determined by the

objective numerical aperture. With the second-order non-linearity ( $\beta = 2$ ), our simulated results qualitatively agree with the experimental data (Figure 6b), and the calculated SHG intensity as functions of excitation wavelength and SiO<sub>2</sub> thickness is shown in Figure 6c. Because the excitation and



**Figure 6.** SHG signal of MoS<sub>2</sub> on different thicknesses of SiO<sub>2</sub> substrates. (a) Typical SHG image of monolayer MoS<sub>2</sub> crystal. (b) Measured and simulated SHG signals under 810 nm excitation. (c) Calculated SHG intensities as functions of excitation wavelength and SiO<sub>2</sub> thickness. Scale bar: 5  $\mu$ m.

emission wavelengths have a fixed 2:1 ratio, the overall interference effect appears to have a broader enhancing region, particularly for SiO<sub>2</sub> thickness within 100–200 nm.

Notice that our simplified model has ignored the reflections at the interfaces of graphene/air and graphene/SiO<sub>2</sub> and multireflections between these interfaces. A more rigorous theory might involve solving the density matrix equation and considering multireflections and interferences of both excitation and emission fields. Nonetheless, we found that our calculations qualitatively agree with the experimental results. Although we did not measure other NLO processes, such as FWM, THG, and TPA, they should in principle fit one of the above three categories and thus could be treated in a similar way. Our model allows a quick estimate of how the substrate thickness and excitation wavelength would affect the NLO signal strength. For example, our approach might partly explain the large differences between  $\chi^{(3)}$  measurements of graphene (using THG) on 300 nm SiO<sub>2</sub> under the excitation wavelengths of 789, 1550, and 1720 nm.<sup>23,43,44</sup> Moreover, microscope objectives with different NAs would affect the intensity profiles of laser focus; thus, additional care needs to be taken when choosing objectives. For instance, high NA objective results in a short Rayleigh range (focal depth) of the focal spot, which will deviate from our plane-wave approximation for the calculation of interference.<sup>38</sup> This is quite different from the linear optics of 2D materials, where the illumination light could be treated as pure plane waves.<sup>37</sup>

Although the contact of SiO<sub>2</sub> and graphene has noticeable doping effect owing to charge exchange at the interface, which shifts the graphene Fermi level,<sup>51,52</sup> it would not affect our results in this study. First of all, the change of the Fermi level induced by SiO<sub>2</sub> doping is around 0.1 V,<sup>51</sup> far below the photon energies used in the measurements and should not significantly alter the NLO signals. Moreover, doping only happens at the graphene/SiO<sub>2</sub> interface, which is expected to cause minimum differences between SiO<sub>2</sub> thickness greater than 100 nm.<sup>53</sup> Our Raman measurements of single-layer graphene on different

SiO<sub>2</sub> thicknesses also indicate that all of the samples used in this study were p-doped (Figure S5).<sup>51</sup>

#### 4. CONCLUSIONS

We have systematically studied the dependence of NLO signals of 2D materials on the thickness of SiO<sub>2</sub> in SiO<sub>2</sub>/Si substrates. Although it might not affect the electrical measurements, we found that it has a great impact on the NLO intensities, mainly through the interference of the incoming and reflected excitation beams. Three major types of NLO processes were investigated, and the theoretical models were given to analyze the experimental data. In general, our results indicate that SiO<sub>2</sub> thickness between 100 and 200 nm would be better suited for most of the NLO measurements under near-infrared light excitation within 700–1100 nm spectral window. The efficiency of NLO signal generations not only determines the sensitivity of these measurements but also critically affects the application of NLO microscopy for studying various 2D materials. Echoing with the substrate-dependent linear optical studies, our work may pave the way to optimize the NLO research for 2D materials and make it more accessible and standard for the community.

#### ■ ASSOCIATED CONTENT

##### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsami.7b09807.

Characterization of NPL and TA properties in graphene; simulated results of graphene NPL and  $\eta(\lambda)$ ; and power dependence of TA and Raman spectra of graphene on different substrates (PDF)

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##### Author Contributions

<sup>†</sup>X.M. and N.X. contributed equally. M.J. and Z.S. conceived the experiment; X.M., Q.L., and W.W. took the optical measurements; and N.X. and H.L. synthesized the samples. The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

##### Notes

The authors declare no competing financial interest.

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